

Biyani's Think Tank

**Concept based notes**

# **Research Method in Management**

BBA

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## Preface



I am glad to present this book, especially designed to serve the needs of the students. The book has been written keeping in mind the general weakness in understanding the fundamental concept of the topic. The book is self-explanatory and adopts the “Teach Yourself” style. It is based on question-answer pattern. The language of book is quite easy and understandable based on scientific approach.

Any further improvement in the contents of the book by making corrections, omission and inclusion is keen to be achieved based on suggestions from the reader for which the author shall be obliged.

I acknowledge special thanks to Mr. Rajeev Biyani, *Chairman* & Dr. Sanjay Biyani, *Director (Acad.)* Biyani Group of Colleges, who is the backbone and main concept provider and also have been constant source of motivation throughout this endeavour. We also extend our thanks to Biyani Shikshan Samiti, Jaipur, who played an active role in co-ordinating the various stages of this endeavour and spearheaded the publishing work.

I look forward to receiving valuable suggestions from professors of various educational institutions, other faculty members and the students for improvement of the quality of the book. The reader may feel free to send in their comments and suggestions to the under mentioned address.

**Author**

# Chapter 1

## Meaning and process of Research

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**Q1. What do you mean by research?**

**Ans.** Research is a thorough, orderly, organized, efficient and logical investigation of an area of knowledge or of a problem. In the broadest sense of the word, the definition of research includes any gathering of data, information and facts for the advancement of knowledge. Main components of a research are:

**1. Curiosity:**

Science is knowledge of the physical or material world gained through observation and experiment. Research begins with a broad question that needs an answer.

**2. Theory (Hypothesis)**

Researcher creates an assumption to be proved or disproved with the help of data.

**3. Experiment**

Researchers design an experiment with steps to test and evaluate the theory (hypothesis) and generate analyzable data. Experiments have controls and a large enough sample group to provide statistically valid results.

**4. Observation**

Observing and recording the results of the experiment generated raw data to prove or disprove the theory.

**5. Analysis**

Statistical analysis on the data and organizing it so that it is understandable generates answers to the initial question. Data may show trends that allow for the broadening of the research.

## 6. Conclusions

Research following the scientific method will either prove or disprove the theory (hypothesis). What happened and why it needs to be explained by the researcher is concluded. Even when a theory (hypothesis) is disproved, valuable data collected in the research may lead to further research. The results are usually published and shared.

**Q2. What are the sources of research problem?**

**Ans.** Sources of research problem are:

- 1 Community
- 2 Own teaching experiences
- 3 Classroom lectures
- 4 Class discussions
- 5 Seminars/workshops/paper presentations
- 6 Internet
- 7 Reading assignments
- 8 Textbooks
- 9 Research reports
- 10 Consultation

**Q3. Explain the process of research.**

**Ans.** Research process includes the following steps:

- **Formulation of research problem**
- **Extensive literature survey**
- **Hypothesis Building**
- **Research Design**
- **Sample design :**
  1. Deliberating Sampling,

2. Simple random sampling
3. Systematic sampling
4. Stratified sampling
5. Cluster sampling
6. Multistage sampling

- **Data Collection**

1. By observation
2. Personal interview
3. Telephone interviews
4. Mailing questionnaires
5. Through schedules

- **Data Analysis**

- **Hypotheses testing**

- **Interpretation**

- **Report Writing**

**Q.4** What are the different components of research Paper?

**Ans**

1. **Title page**
2. **Abstract**
3. **Introduction, or Problem Statement, or Problem Identification:** what exactly is being researched and why; what the relevance or importance is; what questions will be addressed, and an overview of what conclusions will be drawn.
4. **Background and Review of Existing Literature,** including definitions of special terminology used in the paper
5. **Research Methodology: What is Being Studied, and How:** In this section the purpose and research questions or hypotheses are re-stated, and the exact nature of what is being researched and how (population and sampling) is defined, along with what instrumentation was used (copies of instruments should be included in Appendices). Also in this section are details on the procedure and time frame of the research, the analysis plan, the validity and reliability of the data used, the author's assumptions which are based on the research, and possible limitations to these assumptions, or other conclusions.
6. **Data Collection:** This presents the raw data collected via the research methodology described above.

7. **Findings (Results and Analysis of Your Data):** A discussion of what you did and discovered, including why and how you feel it is significant.
8. **Conclusions:** A summary of the nature and application of the "new knowledge" represented in your paper. Also included here are possible contraindications of your conclusions, along with proposed further research based on your findings (and the possible contraindications).
9. **Discussion of 'Limitations':** This section is increasingly a part of research articles published in academic journals. It is a separate section of the paper which describes real or potential faults with the methodology, research material, or other factors that could have influenced the research findings.
10. **Notes** (if needed – usually they are . . . )
11. **Works Cited**, plus a review (where relevant) of related materials which were not cited
12. **Appendices** (if needed), for example to present research instruments which were employed (questionnaires, surveys, statistical data, etc.)

**Q.5**      **How a research problem is formulated?**

**Ans.**      The first step in research process is exploration of the area of interest. This may be done by review of literature and taking expert opinion. An analysis of the situation leads to an understanding of the entire scenario and researcher can identify the research problem

**Q.6.**      **What is the importance of literature review for a researcher?**

**Ans.**      A literature review is a body of text that aims to review the critical points of current knowledge including substantive findings as well as theoretical and methodological contributions to a particular topic. Literature reviews are most often associated with academic-oriented literature, such as a thesis, a literature review usually precedes a research proposal and results section. Its ultimate goal is to bring the reader up to date with current literature on a topic and forms the basis for another goal, such as future research that may be needed in the area.

**Q.7.**      **What do you mean by research hypothesis? Why it is important?**

**Ans.**      A hypothesis is a logical supposition, a reasonable guess. It provides a tentative explanation for a phenomenon under investigation." A hypothesis is important because it guides the researcher. An investigator may refer to the hypothesis to direct his or her thought process toward the solution of the research problem. The hypothesis helps an investigator to collect the right kinds of data needed for the

investigation. Hypotheses are also important because they help an investigator to locate information needed to resolve the research problem. As a hypothesis is continually supported over time by a growing body of data, it becomes a theory. A theory is described as "an organized body of concepts and principles intended to explain a particular phenomenon. Both are supported or rejected on the basis of testing by various investigators under different conditions. An example of a well known theory is Einstein's theory of relativity.

**Q8. What are the types of research design?**

**Ans. The research designs are of the following types:**

- **Exploratory research**

Exploratory research is a type of research conducted for a problem that has not been clearly defined. Exploratory research often relies on secondary research such as reviewing available literature and sometimes on qualitative approaches such as informal discussions with consumers, employees, management or competitors, and more formal approaches through in-depth interviews, focus groups, projective methods, case studies or pilot studies. Results of exploratory research can provide significant insight into a given situation.

- **Descriptive research**

Descriptive research is used to obtain information concerning the current status of the phenomena to describe "**what exists**" with respect to variables or conditions in a situation. The methods involved range from the survey which describes the status quo, the correlation study which investigates the relationship between variables, to developmental studies which seek to determine changes over time. Involves gathering data that describe events and then organizes, tabulates, depicts, and describes the data.

- **Experimental research design**

Experiments are conducted to be able to predict phenomenon. Typically, an experiment is constructed to be able to explain some kind of causation. Experimental research designs are used for the controlled testing of causal processes.

The general procedure is one or more independent variables are manipulated to determine their effect on a dependent variable

- **Qualitative research**

Qualitative research is a method of inquiry employed in many different academic disciplines, traditionally in the social sciences, but also in market research and further contexts. Qualitative researchers aim to gather an in-depth understanding of human behavior and the reasons that govern such behavior. The qualitative method investigates the why and how of decision making, not just what, where, when. Hence, smaller but focused samples are more often needed, rather than large samples.

**Q 9      What are criteria of good research?**

- Research should clearly define.
- The research procedure used should be described in sufficient detail.
- The procedural design of the research should be carefully planned.
- Researcher should report with complete frankness.
- Analysis of data should be sufficiently adequate.
- Conclusion should be confined

## Chapter 2

# Motivational Research

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**Q1. What do you mean by Motivational Research?**

**Ans.** Any research that attempts to explore the area of motivation of people can be called motivational research. Motivational research is a type of marketing research that attempts to explain why consumers behave as they do. Implicitly, motivational research assumes the existence of underlying or unconscious motives that influence consumer behavior. Motivational research attempts to identify forces and influences that consumers may not be aware of (e.g., cultural factors, sociological forces). Typically, these unconscious motives (or beyond-awareness reasons) are intertwined with and complicated by conscious motives, cultural biases, economic variables, and fashion trends (broadly defined). Motivational research attempts to sift through all of these influences and factors to unravel the mystery of consumer behavior as it relates to a specific product or service, so that the marketer better understands the target audience and how to influence that audience.

### **The Major Techniques**

The three major motivational research techniques are **observation, focus groups, and depth interviews**. Observation can be a fruitful method of deriving hypotheses about human motives. Anthropologists have pioneered the development of this technique. All of us are familiar with anthropologists living with the “natives” to understand their behavior. This same systematic observation can produce equally insightful results about consumer behavior. Observation can be accomplished in-person or sometimes through the convenience of video. Usually, personal observation is simply too expensive, and most consumers don't want an anthropologist living in their household for a month or two.

### **The Focus Group Interviews**

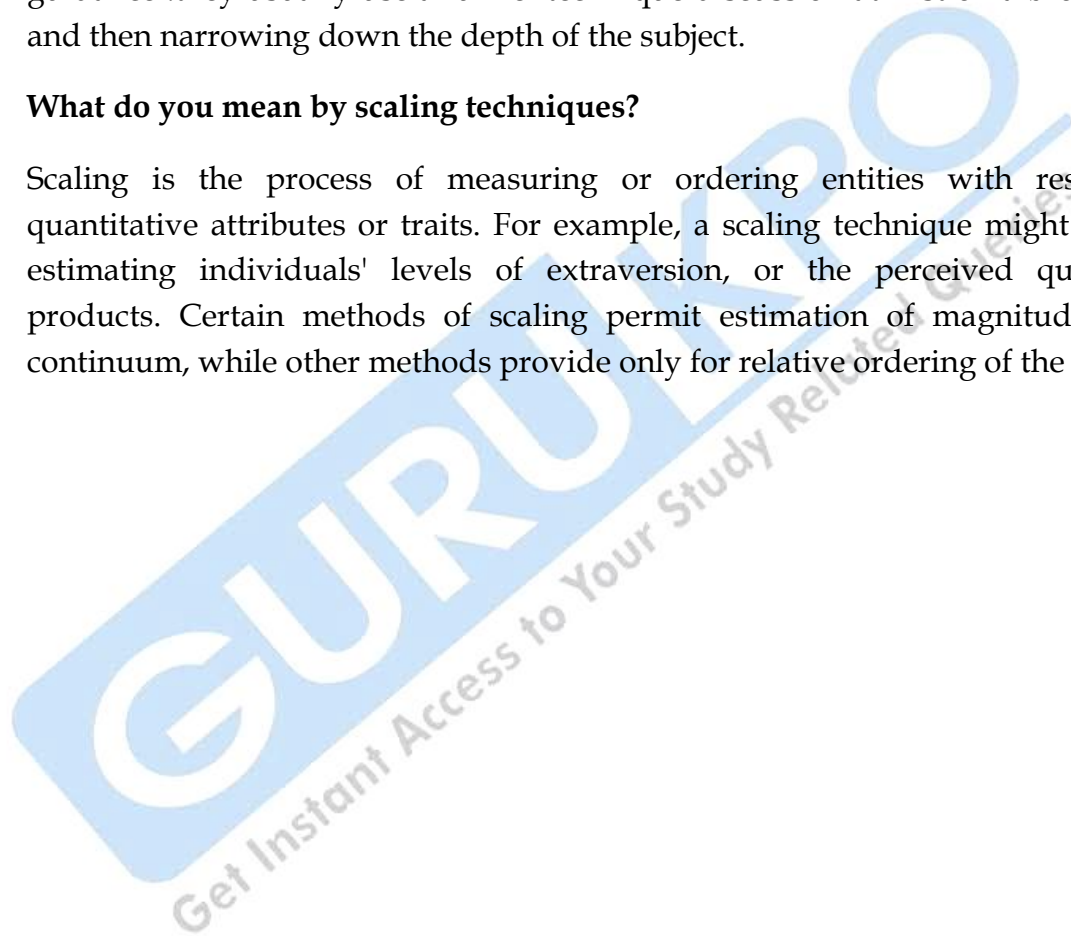
These involve interviews of a group of 8-12 individuals lasting about one and half hours. the discussion is led by a moderator who keeps the focus on the desired topic.

### **The Depth Interview**

This entails interviews lasting from one to three hours and needing expert guidance. they usually use a funnel technique discussion at first on a broad level and then narrowing down the depth of the subject.

**Q2. What do you mean by scaling techniques?**

**Ans.** Scaling is the process of measuring or ordering entities with respect to quantitative attributes or traits. For example, a scaling technique might involve estimating individuals' levels of extraversion, or the perceived quality of products. Certain methods of scaling permit estimation of magnitudes on a continuum, while other methods provide only for relative ordering of the entities.



## Chapter 3

# Sampling Design

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**Q1.** What do you mean by sample design?

**Ans.** **sampling** is concerned with the selection of a subset of individuals from within a statistical population to estimate characteristics of the whole population. the selected respondents constitute what is technically called a sample and the selection process is called sampling techniques.

**Q2.** What are the steps involved in sampling process?

**The sampling process comprises several stages:**

- Defining the population of concern
- Specifying a sampling frame, a set of items or events possible to measure
- Specifying a sampling method for selecting items or events from the frame
- Determining the sample size
- Implementing the sampling plan
- Sampling and data collecting

**Q3** What are the criteria of selecting a sample procedure?

**Ans.** Researcher must consider two reasons of the incorrect inferences. Systematic bias and sampling error. A systematic bias cannot be reduced or eliminated by increasing sample size because it results from errors in the sampling procedure. It is the result of following factors

- Defective measuring device
- Non respondent
- Inappropriate sampling frame

- Natural bias in reporting data  
Sample errors are the random variations in the sample estimates around the true population parameters. Sampling errors decrease or increase in the size of sample and it happens to be smaller magnitude in case of homogeneous population.

**Q4 . What are the various sampling methods?**

Ans. Sampling methods are as follows:

#### **Probability and non probability sampling**

A **probability sampling** scheme is one in which every unit in the population has a chance (greater than zero) of being selected in the sample, and this probability can be accurately determined. The combination of these traits makes it possible to produce unbiased estimates of population totals, by weighting sampled units according to their probability of selection.

**Non probability sampling** is any sampling method where some elements of the population have *no* definite chance of selection, or where the probability of selection can't be accurately determined. Probability sampling may be of the following types:

#### **Simple random sampling**

In a simple random sample ('SRS') of a given size, all such subsets of the frame are given an equal probability. Each element of the frame thus has an equal probability of selection: the frame is not subdivided or partitioned. This minimizes bias and simplifies analysis of results.

#### **Systematic sampling**

Systematic sampling relies on arranging the target population according to some ordering scheme and then selecting elements at regular intervals through that ordered list. Systematic sampling involves a random start and then proceeds with the selection of every  $k$ th element from then onwards. In this case,  $k = (\text{population size} / \text{sample size})$ . It is important that the starting point is not automatically the first in the list, but is instead randomly chosen from within the first to the  $k$ th element in the list. A simple example would be to select every 10th name from the telephone directory (an 'every 10th' sample, also referred to as 'sampling with a skip of 10').

### **Stratified sampling**

Where the population embraces a number of distinct categories, the frame can be organized by these categories into separate "strata." Each stratum is then sampled as an independent sub-population, out of which individual elements can be randomly selected. Dividing the population into distinct, independent strata can enable researchers to draw inferences about specific subgroups that may be lost in a more generalized random sample.

### **Cluster sampling**

It is an example of 'two-stage sampling' or 'multistage sampling': in the first stage a sample of areas is chosen; in the second stage a sample of respondents *within* those areas is selected.

**Multistage sampling** Multistage sampling is a complex form of cluster sampling in which two or more levels of units are embedded one in the other. The first stage consists of constructing the clusters that will be used to sample from. In the second stage, a sample of primary units is randomly selected from each cluster (rather than using all units contained in all selected clusters). In following stages, in each of those selected clusters, additional samples of units are selected, and so on. All ultimate units (individuals, for instance) selected at the last step of this procedure are then surveyed.

This technique, thus, is essentially the process of taking random samples of preceding random samples. It is not as effective as true random sampling, but it probably solves more of the problems inherent to random sampling. Moreover, it is an effective strategy because it banks on multiple randomizations. As such, it is extremely useful.

Multistage sampling is used frequently when a complete list of all members of the population does not exist and is inappropriate. Moreover, by avoiding the use of all sample units in all selected clusters, multistage sampling avoids the large, and perhaps unnecessary, costs associated traditional cluster sampling.

### **Non Probability sampling:**

**Quota sampling**, in **quota sampling** the population is first segmented into mutually exclusive sub-groups, just as in stratified sampling. Then judgment is used to select the subjects or units from each segment based on a specified proportion. It is this second step which makes the technique one of non-probability sampling. In quota sampling the selection of the sample is non-random. For example interviewers might be tempted to interview those who look most helpful. The problem is that these samples may be biased because not everyone gets a chance of selection. This random element is its greatest weakness and quota versus probability has been a matter of controversy for many years.

**Convenience sampling** (sometimes known as **grab** or **opportunity sampling**) is a type of non probability sampling which involves the sample being drawn from that part of the population which is close to hand. That is, a sample population selected because it is readily available and convenient. It may be through meeting the person or including a person in the sample when one meets them or chosen by finding them through technological means such as the internet or through phone. The researcher using such a sample cannot scientifically make generalizations about the total population from this sample because it would not be representative enough. For example, if the interviewer was to conduct such a survey at a shopping center early in the morning on a given day, the people that he/she could interview would be limited to those given there at that given time, which would not represent the views of other members of society in such an area, if the survey was to be conducted at different times of day and several times per week. This type of sampling is most useful for pilot testing.

## Chapter 4

# Data Collection

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**Q1 . Differentiate between primary and secondary data.**

**Ans. Primary and Secondary Data:**

Primary data are collected by the investigator through field survey. Such data are in raw form **and** must be refined before use. **On** the other hand, secondary data are extracted from the existing published or unpublished sources.

**Q2. What do you mean by sampling?**

**Ans. Sampling** is that part of statistical practice concerned with the selection of a subset of individual observations within a population of individuals intended to yield some knowledge about the population of concern, especially for the purposes of making predictions based on statistical inference.

**Q3 . What are the sources of secondary data collection?**

**Ans. Secondary data** are the other people's statistics, where other people includes governments at all levels, international bodies or institutions like IMF, IBRD, etc., or other countries, private and government research organizations, Reserve Bank of India and other banks, research scholars of repute, etc. Broadly speaking we can divide the sources of secondary data into two categories: published sources and unpublished SOW.

**A) Published Sources**

- 1) Official publications of the government at all levels - Central, State, Union
- 2) Official publications of foreign countries.
- 3) Official publications of international bodies like IMF, UNESCO, WHO, etc.
- 4) Newspapers and Journals of repute, both local and international.
- 5) Official publications of RBI, and other Banks, LIC, Trade Unions, Stock Exchange, Chambers of Commerce, etc.
- 6) Reports submitted by reputed economists, research scholars, universities, commissions of inquiry, if made public. Some main sources of published data in India are:

**Central Statistical Organization (C.S.O.):** It publishes data on national income, savings, capital formation, etc. in a publication called National Accounts Statistics.

**National Sample Survey Organization (N.S.S.O.):** Under Ministry of Statistics and Programme Implementation, this organization provides us **data** on all aspects of national economy, such as agriculture, industry, labor and Consumption expenditure.

**Reserve Bank of India Publications (R.B.I.):** It publishes financial statistics. Its publications are Report on Currency and Finance, Reserve Bank of India Bulletin, Statistical Tables Relating to Banks in India, etc.

**B) Un-published Sources**

- 1) Unpublished findings of certain inquiry committees.
- 2) Research workers' findings.
- 3) Unpublished material found with Trade Associations, Labor Organizations and Chambers of Commerce.

**Q4 . What are the differences between questionnaires and schedules?**

**Ans**

<b>Questionnaire</b>	<b>Schedules</b>
Sent through the mail to the respondents	Generally filled out by the researcher or the enumerator
Collection of data relative cheap and economical	Relatively more expensive
Non responses usually high	Non responses very low
Identity of respondent is unknown	Identity of respondent is known
Slow collection of data	Fast collection of data
Success of methods depends on the questionnaire	Success of methods depends on the honesty and competency of the enumerator.
Not possible	Observation method can also be used with this method
Risk of collecting incomplete and wrong information more	More accurate.

**Q5 . What are the methods of primary data collection?**

**Ans. COLLECTION OF PRIMARY DATA - SURVEY TECHNIQUES**

**After** the investigator is convinced that the gain from primary data outweighs the money cost, effort and time, she/he can go in for this. She/he can use any of the following methods to collect primary data:

- a) Direct Personal Investigation
- b) Indirect Oral Investigation
- c) Use of Local Reports
- d) Questionnaire method

**a) Direct Personal Investigation**

Here the investigator collects information personally from the respondents. She/he meets them personally to collect information. This method requires much from the investigator such as:

- 1) She/he should be polite, unbiased and tactful.
- 2) She/he should know the local conditions, customs and traditions
- 3) She/he should be intelligent possessing good observation power.
- 4) She/he should use simple, easy and meaningful questions to extract information.

This method is suitable only for intensive investigations. It is a costly method in terms of money, effort and time. Further, the personal bias of the investigator cannot be ruled out and it can do a lot of harm to the investigation.

**b) Indirect Oral Investigation Method**

This method is generally used when the respondents are reluctant to part with the information due to various reasons. Here, the information is collected from a witness or from a third party who are directly or indirectly related to the problem and possess sufficient knowledge. The person(s) who is/are selected as informants must possess the following qualities:

- 1) They should possess full knowledge about the issue.
- 2) They must be willing to reveal it faithfully and honestly.
- 3) They should not be biased and prejudiced.
- 4) They must be capable of expressing themselves to the true spirit of the inquiry.

**c) Questionnaire Method**

It is the most important and systematic method of collecting **primary** data, especially when the inquiry is quite extensive. It involves preparation of a list of questions relevant to the **inquiry** and presenting them in the form of a booklet, often called a questionnaire. The questionnaire is divided into two parts:

- 1) General introductory part which contains questions regarding the identity of the respondent and contains information such as name, address, telephone number, qualification, profession, etc.
- 2) Main question part containing questions connected with the inquiry. These questions differ from inquiry to inquiry. Preparation of the questionnaire is a highly specialized job and is perfected with experience. Therefore, some experienced persons should be associated with it.

**Q6. What do you mean by projective techniques?**

**Ans.** Projective techniques also called indirect interview techniques for the collection of data have been developed by the psychologist to use the projection of respondent for inferring about underlying motive, urges or intention which are such that the respondents either resist to reveal them or unable to figure out himself.

**Important Projective techniques**

- Word association test
- Story completion test
- Verbal projection test
- Play technique
- Quiz and test and examination
- Sociometry

## Chapter 5

# Presentation of Data

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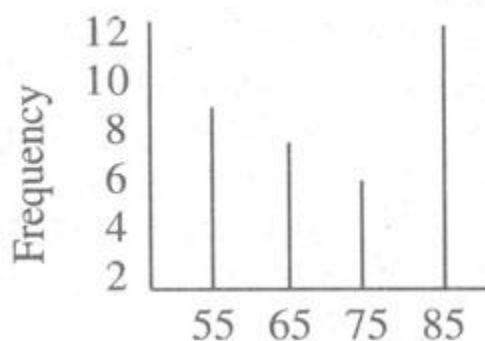
**Q1 .** What is the use of tables and graphs?

**Ans.** When significant amounts of quantitative data are presented in a report or publication, it is most effective to use tables and/or graphs. Tables permit the actual numbers to be seen most clearly, while graphs are superior for showing trends and changes in the data

**Q2.** What is Line Diagram?

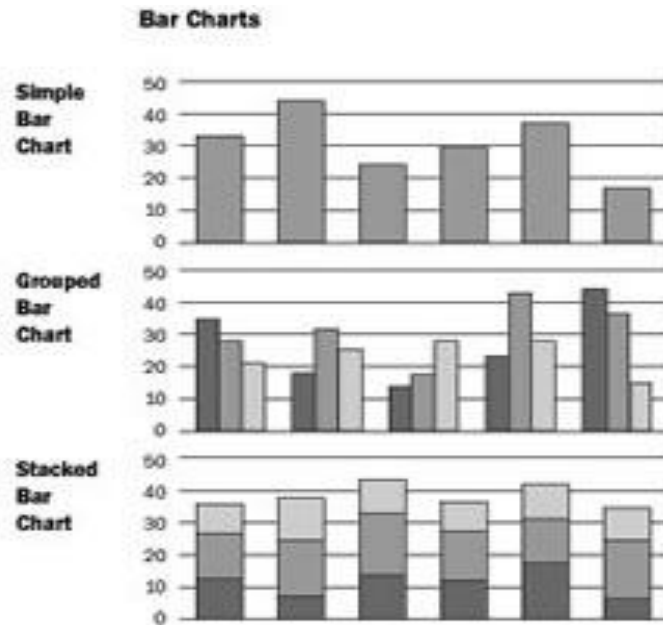
### Line diagram

Of all forms of graphic presentation of statistical data line diagram is the simplest one. A line diagram is one in which the frequency distribution is presented in the form of a series of lines in a graph sheet. The heights of these lines are equal to or in proportion to the frequencies of the class. The lines are erected at the midpoints of the class intervals.



Q3. Show various types of Bar Charts.

Ans



Q4. Explain the construction of Pie Chart.

How to Use a Pie Chart

Pie Chart



**Step 1.** Taking the data to be charted, calculate the percentage contribution for each category. First, total all the values. Next, divide the value of each category by the total. Then, multiply the product by 100 to create a percentage for each value.

**Step 2.** Draw a circle. Using the percentages, determine what portion of the circle will be represented by each category. This can be done by eye or by calculating the number of degrees and using a compass. By eye, divide the circle into four quadrants, each representing 25 percent.

**Step 3.** Draw in the segments by estimating how much larger or smaller each category is. Calculating the number of degrees can be done by multiplying the percent by 3.6 (a circle has 360 degrees) and then using a compass to draw the portions.

**Step 4.** Provide a title for the pie chart that indicates the sample and the time period covered by the data. Label each segment with its percentage or proportion (e.g., 25 percent or one quarter) and with what each segment represents (e.g., people who returned for a follow-up visit; people who did not return).



## Chapter 6

### Testing of Hypotheses

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**Q1 . What is hypotheses?**

**Ans.** Research hypotheses are the predictive statement capable of being tested by scientific methods that relates an independent variable to some dependent variable. For example "the automobile A is performing as well as automobile B"

**Q2. Explain the null and alternative hypotheses?**

**Ans.** If we are compare method A with method B about its superiority and if we precede on the assumption of that both method equally good, then this assumption is termed as Null hypotheses. As against this we may think that method a superior or the method B is inferior then it is termed as alternative hypotheses.

A null hypothesis is "symbolized as  $H_0$ ".

The alternate, or research, hypothesis, "symbolized as  $H_1$ ".





**Q3 . Discuss the TYPE I and TYPE II error?**

**Ans.** There are two types of error that researchers are concerned with: Type I and Type II. A Type I error occurs when the results of research show that a difference exists but in reality there is no difference. This is directly related to alpha in that alpha was likely set too high and therefore lowering the amount of acceptable error would reduce the chances of a Type I error.

Lowering the amount of acceptable error, however, also increases the chances of a Type II error, which refers to the acceptance of the null hypothesis when in fact the alternative is true. When there is a significant difference in the population but we fail to find this difference, our study is said to lack power. Power, abbreviated with the upper case beta ( $\beta$ ), refers to a study's strength to find a difference when a difference actually exists. In other words, the greater the chances of a Type I

error, the less likely a Type II error, and vice versa. These two errors are summarized in Figure 9.1

Figure 9.1: Type I and Type II Errors

HYPOTHESIS TESTING OUTCOMES		Reality	
		The Null Hypothesis Is True	The Alternative Hypothesis is True
R e s e a r c h	The Null Hypothesis Is True	Accurate $1 - \alpha$ 	Type II Error $\beta$ 
	The Alternative Hypothesis is True	Type I Error $\alpha$ 	Accurate $1 - \beta$ 

**Q4. Explain the two tailed and one tailed test?**

**Ans** Suppose we have a null hypothesis  $H_0$  and an alternative hypothesis  $H_1$ . We consider the distribution given by the null hypothesis and perform a test to determine whether or not the null hypothesis should be rejected in favors of the alternative hypothesis.

There are two different types of tests that can be performed. A **one-tailed** test looks for an increase or decrease in the parameter whereas a **two-tailed** test looks for any change in the parameter (which can be any change- increase or decrease).

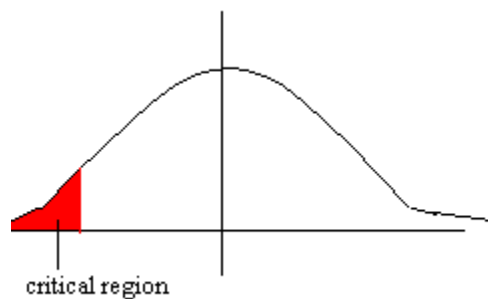
We can perform the test at any level (usually 1%, 5% or 10%). For example, performing the test at a 5% level means that there is a 5% chance of wrongly rejecting  $H_0$ .

If we perform the test at the 5% level and decide to reject the null hypothesis, we say "there is significant evidence at the 5% level to suggest the hypothesis is false".

### One-Tailed Test

We choose a critical region. In a one-tailed test, the critical region will have just one part (the red area below). If our sample value lies in this region, we reject the null hypothesis in favour of the alternative.

Suppose we are looking for a definite decrease. Then the critical region will be to the left. Note, however, that in the one-tailed test the value of the parameter can be as high as you like.



### Example

Suppose we are given that  $X$  has a Poisson distribution and we want to carry out a hypothesis test on the mean,  $\lambda$ , based upon a sample observation of 3.

Suppose the hypotheses are:

$$H_0: \lambda = 9$$

$$H_1: \lambda < 9$$

We want to test if it is "reasonable" for the observed value of 3 to have come from a Poisson distribution with parameter 9. So what is the probability that a value as low as 3 has come from a  $Po(9)$ ?

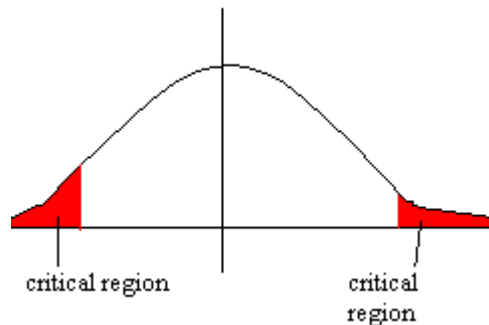
$$P(X \leq 3) = 0.0212 \text{ (this has come from a Poisson table)}$$

The probability is less than 0.05, so there is less than a 5% chance that the value has come from a  $Poisson(3)$  distribution. We therefore reject the null hypothesis in favour of the alternative at the 5% level.

However, the probability is greater than 0.01, so we would not reject the null hypothesis in favour of the alternative at the 1% level.

## Two-Tailed Test

In a two-tailed test, we are looking for either an increase or a decrease. So, for example,  $H_0$  might be that the mean is equal to 9 (as before). This time, however,  $H_1$  would be that the mean is not equal to 9. In this case, therefore, the critical region has two parts:



### Example

Lets test the parameter  $p$  of a Binomial distribution at the 10% level.

Suppose a coin is tossed 10 times and we get 7 heads. We want to test whether or not the coin is fair. If the coin is fair,  $p = 0.5$ . Put this as the null hypothesis:

$$H_0: p = 0.5$$

$$H_1: p \neq 0.5$$

Now, because the test is 2-tailed, the critical region has two parts. Half of the critical region is to the right and half is to the left. So the critical region contains both the top 5% of the distribution and the bottom 5% of the distribution (since we are testing at the 10% level).

If  $H_0$  is true,  $X \sim \text{Bin}(10, 0.5)$ .

If the null hypothesis is true, what is the probability that  $X$  is 7 or above?

$$P(X \geq 7) = 1 - P(X < 7) = 1 - P(X \leq 6) = 1 - 0.8281 = 0.1719$$

Is this in the critical region? No- because the probability that  $X$  is at least 7 is not less than 0.05 (5%), which is what we need it to be.

So there is not significant evidence at the 10% level to reject the null hypothesis.

**Q5 Discuss the procedure of hypothesis testing.**

Ans. Testing Procedure:.

1. The first step is to state the relevant null and alternative hypotheses. whether the alternative hypothesis can either be accepted or stays undecided as it was before the test.
2. The second step is to consider the statistical assumptions being made about the sample in doing the test; for example, assumptions about the statistical independence or about the form of the distributions of the observations. 4. Decide which test is appropriate, and stating the relevant test statistic .
- 3 Derive the distribution of the test statistic under the null hypothesis from the assumptions. For example the test statistics may follow a Student's t distribution or a normal distribution.
4. The distribution of the test statistic partitions the possible values of T into those for which the null-hypothesis is rejected, the so called critical region, and those for which it is not.
7. Compute from the observations the observed value of the test statistic .
8. Decide to either fail to reject the null hypothesis or reject it in favor of the alternative. The decision rule is to reject the null hypothesis  $H_0$  if the observed value is in the critical region, and to accept or "fail to reject" the hypothesis otherwise.

## Chapter 6

# Analysis of Data

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**Q1. What do you mean by Correlation?**

**Ans.** In statistics and probability theory, correlation means how closely related two sets of data are.

Correlation does not always mean that one causes the other. It is very possible that there is a third factor involved.

Correlation usually has one of two directions. These are positive or negative. If it is positive, then the two sets go up together. If it is negative, then one goes up while the other goes down.

Lots of different measurements of correlation are used for different situations. For example on a scatter graph, people draw a line of best fit to show the direction of the correlation

**Q2. Write down the formula for calculating the correlation coefficient and explain its calculation**

**Ans**

The formula for the correlation is:

$$r = \frac{N\sum xy - (\sum x)(\sum y)}{\sqrt{[N\sum x^2 - (\sum x)^2][N\sum y^2 - (\sum y)^2]}}$$

Where:

- N = number of pairs of scores  
 $\sum xy$  = sum of the products of paired scores  
 $\sum x$  = sum of x scores  
 $\sum y$  = sum of y scores  
 $\sum x^2$  = sum of squared x scores  
 $\sum y^2$  = sum of squared y scores

We use the symbol **r** to stand for the correlation.

### Example

Person	Height (x)	Self Esteem (y)	x*y	x*x	y*y
1	68	4.1	278.8	4624	16.81
2	71	4.6	326.6	5041	21.16
3	62	3.8	235.6	3844	14.44
4	75	4.4	330	5625	19.36
5	58	3.2	185.6	3364	10.24
6	60	3.1	186	3600	9.61
7	67	3.8	254.6	4489	14.44
8	68	4.1	278.8	4624	16.81
9	71	4.3	305.3	5041	18.49
10	69	3.7	255.3	4761	13.69

11	68	3.5	238	4624	12.25
12	67	3.2	214.4	4489	10.24
13	63	3.7	233.1	3969	13.69
14	62	3.3	204.6	3844	10.89
15	60	3.4	204	3600	11.56
16	63	4	252	3969	16
17	65	4.1	266.5	4225	16.81
18	67	3.8	254.6	4489	14.44
19	63	3.4	214.2	3969	11.56
20	61	3.6	219.6	3721	12.96
<b>Sum =</b>	<b>1308</b>	<b>75.1</b>	<b>4937.6</b>	<b>85912</b>	<b>285.45</b>

$$\begin{aligned}
 N &= 20 \\
 \Sigma xy &= 4937.6 \\
 \Sigma x &= 1308 \\
 \Sigma y &= 75.1 \\
 \Sigma x^2 &= 85912 \\
 \Sigma y^2 &= 285.45
 \end{aligned}$$

Now, when we plug these values into the formula given above, we get the following

$$r = \frac{20(4937.6) - (1308)(75.1)}{\sqrt{[20(85912) - (1308*1308)][20(285.45) - (75.1*75.1)]}}$$

$$r = \frac{98752 - 98230.8}{\sqrt{[1718240 - 1710864][5709 - 5640.01]}}$$

$$r = \frac{521.2}{\sqrt{[7376][68.99]}}$$

$$r = \frac{521.2}{\sqrt{508870.2}}$$

$$r = \frac{521.2}{713.3514}$$

$$r = .73$$

**Q3. Discuss the concept of simple regression.**

**Ans.** Simple regression is used to examine the relationship between one dependent and one independent variable. After performing an analysis, the regression statistics can be used to predict the dependent variable when the independent variable is known. Regression goes beyond correlation by adding prediction capabilities.

For example, a medical researcher might want to use body weight (independent variable) to predict the most appropriate dose for a new drug (dependent variable). The purpose of running the regression is to find a formula that fits the relationship between the two variables. The regression line (known as the least squares line) is a plot of the expected value of the dependent variable for all values of the independent variable. Technically, it is the line that "minimizes the

squared residuals". The regression line is the one that best fits the data on a scatter plot.

Using the regression equation, the dependent variable may be predicted from the independent variable. The slope of the regression line (b) is defined as the rise divided by the run. The y intercept (a) is the point on the y axis where the regression line would intercept the y axis. The slope and y intercept are incorporated into the regression equation. The intercept is usually called the constant, and the slope is referred to as the coefficient. Since the regression model is usually not a perfect predictor, there is also an error term in the equation.

In the regression equation, y is always the dependent variable and x is always the independent variable. Here are three equivalent ways to mathematically describe a linear regression model.

$$y = \text{intercept} + (\text{slope } x) + \text{error}$$

$$y = \text{constant} + (\text{coefficient } x) + \text{error}$$

$$y = a + bx + e$$

**Q4. Discuss the calculation of regression equation.**

**Ans**

In the table below, the  $x_i$  column shows scores on the aptitude test. Similarly, the  $y_i$  column shows statistics grades. The last two rows show sums and mean scores that we will use to conduct the regression analysis.

	Student	$x_i$	$y_i$	$(x_i - \bar{x})$	$(y_i - \bar{y})$	$(x_i - \bar{x})^2$	$(y_i - \bar{y})^2$	$(x_i - \bar{x})(y_i - \bar{y})$
1	95	85	17	8	289	64	136	
2	85	95	7	18	49	324	126	
3	80	70	2	-7	4	49	-14	

	4	70	65	-8	-12	64	144	96
	5	60	70	-18	-7	324	49	126
<b>Sum</b>		390	385			730	630	470
<b>Mean</b>		78	77					

The regression equation is a linear equation of the form:  $\hat{y} = b_0 + b_1x$ . To conduct a regression analysis, we need to solve for  $b_0$  and  $b_1$ . Computations are shown below.

$b_1 = \frac{\sum [(x_i - \bar{x})(y_i - \bar{y})]}{\sum [(x_i - \bar{x})^2]}$ $b_1 = 470/730 = 0.644$	$b_0 = \bar{y} - b_1 * \bar{x}$ $b_0 = 77 - (0.644)(78) = 26.768$
--	---

Therefore, the regression equation is:  $\hat{y} = 26.768 + 0.644x$ .

**Q5. What are the measures of Central Tendency?**

Ans. Measures of Central Tendency show the tendency of data to cluster around a central value. They give us a single value that represents the whole series of data. Following are the measures of central tendency:

**Mean**

The **mean** (or average) of a set of data values is the sum of all of the data values divided by the number of data values. That is:

$$\text{Mean} = \frac{\text{Sum of all data values}}{\text{Number of data values}}$$

Symbolically,

$$\bar{x} = \frac{\sum x}{n}$$

where  $\bar{x}$  (read as 'x bar') is the mean of the set of  $x$  values,

$\sum x$  is the sum of all the  $x$  values, and

$n$  is the number of  $x$  values.

### Example 1

The marks of seven students in a mathematics test with a maximum possible mark of 20 are given below:

15 13 18 16 14 17 12

Find the mean of this set of data values.

Solution:

$$\begin{aligned} \text{Mean} &= \frac{\text{Sum of all data values}}{\text{Number of data values}} \\ &= \frac{15+13+18+16+14+17+12}{7} \\ &= \frac{105}{7} \\ &= 15 \end{aligned}$$

So, the mean mark is 15.

Symbolically, we can set out the solution as follows:

$$\begin{aligned}\bar{x} &= \frac{\sum x}{n} \\ &= \frac{15+13+18+16+14+17+12}{7} \\ &= \frac{105}{7} \\ &= 15\end{aligned}$$

So, the mean mark is 15.

### Median

The **median** of a set of data values is the middle value of the data set when it has been arranged in ascending order. That is, from the smallest value to the highest value.

#### Example 2

The marks of nine students in a geography test that had a maximum possible mark of 50 are given below:

47 35 37 32 38 39 36 34 35

Find the median of this set of data values.

Solution:

Arrange the data values in order from the lowest value to the highest value:

32 34 35 35 36 37 38 39 47

The fifth data value, 36, is the middle value in this arrangement.

$\therefore$  Median = 36

*Note:*

The number of values,  $n$ , in the data set = 9

$$\begin{aligned}\text{Median} &= \frac{1}{2}(9+1) \text{ th value} \\ &= 5\text{th value} \\ &= 36\end{aligned}$$

*In general:*

$$\text{Median} = \frac{1}{2}(n+1) \text{ th value, where } n \text{ is the number of data values in the sample}$$

If the number of values in the data set is even, then the **median** is the average of the two middle values.

### Example 3

Find the median of the following data set:  
12 18 16 21 10 13 17 19

Solution:

Arrange the data values in order from the lowest value to the highest value:  
10 12 13 16 17 18 19 21

The number of values in the data set is 8, which is even. So, the median is the average of the two middle values.

$$\begin{aligned}\therefore \text{Median} &= \frac{4\text{th data value} + 5\text{th data value}}{2} \\ &= \frac{16+17}{2} \\ &= \frac{33}{2} \\ &= 16.5\end{aligned}$$

*Alternative way:*

There are 8 values in the data set.

$$\therefore n = 8$$

$$\begin{aligned}\text{Now, median} &= \left(\frac{n+1}{2}\right)\text{th value} \\ &= \left(\frac{8+1}{2}\right) \\ &= \frac{9}{2} \\ &= 4.5\text{th value}\end{aligned}$$

The fourth and fifth scores, 16 and 17, are in the middle. That is, there is no one middle value.

$$\begin{aligned}\therefore \text{Median} &= \frac{16+17}{2} \\ &= \frac{33}{2} \\ &= 16.5\end{aligned}$$

*Note:*

- Half of the values in the data set lie below the median and half lie above the median.
- The median is the most commonly quoted figure used to measure property prices. The use of the median avoids the problem of the mean property price which is affected by a few expensive properties that are not representative of the general property market.

### Mode

The **mode** of a set of data values is the value(s) that occurs most often.

The mode has applications in printing. For example, it is important to print more of the most popular books; because printing different books in equal numbers would cause a shortage of some books and an oversupply of others.

Likewise, the mode has applications in manufacturing. For example, it is important to manufacture more of the most popular shoes; because manufacturing different shoes in equal numbers would cause a shortage of some shoes and an oversupply of others.

### Example 1

Find the mode of the following data set:

48 44 48 45 42 49 48

Solution:

The mode is 48 since it occurs most often.

Note:

- It is possible for a set of data values to have more than one mode.
- If there are two data values that occur most frequently, we say that the set of data values is **bimodal**.
- If there is no data value or data values that occur most frequently, we say that the set of data values has no mode.

**Q6 .Calculate Mean Median and Mode in frequency distribution.**

X	Frequency	Mean	Freq * Mean
Age 41-43	1	42	42
Group 38-40	3	39	117
35-37	4	36	144
32-34	4	33	132
29-31	5	30	150
26-28	8	27	216
23-25	10	24	240
20-22	18	21	378
17-19	23	18	414
14-16	17	15	255

$$\begin{array}{l} 11-13 \quad 10 \quad 12 \quad 120 \\ S = 103 \quad S = 2,208 \end{array}$$

$$\text{Mean} = \bar{X} = \frac{2208}{103} = 21.44$$

Then the mean  $\bar{X}$  is defined as

$$\bar{X} = \frac{\sum_{i=1}^n (f_i X_i)}{\sum_{i=1}^n f_i} = \frac{X_1 f_1 + X_2 f_2 + X_3 f_3 + \dots + X_n f_n}{f_1 + X_2 f_2 + X_3 f_3 + \dots + X_n f_n}$$

**(2) The Median:**

If  $X_1, X_2, X_3, \dots, X_n$  is a set of data arranged in ascending order of magnitude, then the median of the set of data is given by :

$M_e = X_{(n+1)/2}$ , if n is odd,

$M_e = (X_{n/2} + X_{(n/2+1)})/2$ , if n is even.

This result is true also for an ungrouped frequency distribution. If the data is a grouped frequency distribution, then the median,

$M_e = l_1 + ((N/2 - c)/f) * (l_2 - l_1)$

where  $N = (f_1 + f_2 + f_3 + \dots + f_n)$

$l_1 - l_2$  = The median class

f = Cumulative Frequency of the median class

c = Cumulative Frequency of the class preceding the median class

X	Cumulative Freq	Frequency (Less Than)
Age 11-13	10	10
Group 14-16	17	27
17-19	23	50 <--- Modal Class
20-22	18	68 <--- Median Class
23-25	10	78
26-28	8	86 Median = 103/2=51.5
29-31	5	91
32-34	4	95
35-37	4	99
38-40	3	102
41-43	1	103

$$S=103$$

Median Class Lower Bound = 11 = 20

Median Class Upper Bound = 12 = 22

N = 103, 12 - 11 = 2, f = 68, c = 50

$$\text{Median} = 20 + ((103/2 - 50)/68)*2 = 20.0441$$

### (3) The Mode:

For a grouped frequency distribution, the mode is given by

$$M_o = l_1 + ((f_1 - f_0)/(2f_1 - f_0 - f_2))*(l_2 - l_1)$$

where:

$l_1 - l_2$  = the modal class

$f_1$  = frequency of the modal class

$f_2$  = Frequency of the class following the modal class

$f_0$  = Frequency of the class following the modal class

$$l_2 - l_1 = (17-19) = 2, f_1 = 23, f_0 = 17, f_2 = 18$$

$$M_o = 17 + ((23-17)/(2*23-17-18))*(2) = 17 + (6/11)*2 = 18.091$$

**Q7. What are the requisites of a good measure of central tendency?**

Ans.

### **REQUISITES OF A GOOD AVERAGE OR MEASURE OF CENTRAL TENDENCY**

According to Prof. Yule, the following are the requirements to be satisfied by an ideal average or measure of central tendency.

- It should be rigidly defined.
- It should be easy to understand and calculate.
- It should be based on all the observations.
- It should be suitable for further mathematical treatment.
- It should be affected as little as possible by fluctuations of sampling.
- It should not be affected much by extreme observations.

**Q8. What are the measures of Dispersion?**

Ans. Measures of dispersion show the variability of data from the central value. The measures of dispersion describe the width of the distribution

### **Measures of Dispersion**

#### **Range**

The range,  $R$ , of the data is the difference of the highest and smallest values being analyzed.

Example {1, 3, 8, 3, 7, 11, 8, 3, 9, 10}

$$R = 11 - 1 = 10$$

### Deviation

The deviation is the difference of each value from the mean. This is used in the calculation of the standard deviation and variance. "x" is the point of interest. The sum of deviations from the mean is always zero.

### Standard Deviation

The standard deviation is shown by the following formulas. It also equals the square root of the variance. "x" is the point of interest.

"n" represent the sample size,

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x - \bar{x})^2}$$

### Variance

The variance is the standard deviation squared.

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x - \bar{x})^2$$

### Example

An owner of a restaurant is interested in how much people spend at the restaurant. He examines 10 randomly selected receipts for parties of four and writes down the following data.

44, 50, 38, 96, 42, 47, 40, 39, 46, 50

He calculated the mean by adding and dividing by 10 to get

$$x = 49.2$$

Below is the table for getting the standard deviation:

x	x - 49.2	(x - 49.2) <sup>2</sup>
44	-5.2	27.04
50	0.8	0.64
38	11.2	125.44
96	46.8	2190.24
42	-7.2	51.84
47	-2.2	4.84
40	-9.2	84.64
39	-10.2	104.04
46	-3.2	10.24
50	0.8	0.64
<b>Total</b>		<b>2600.4</b>

Now

$$\frac{2600.4}{10 - 1} = 288.7$$

Hence the variance is 289 and the standard deviation is the square root of 289 = 17. One of the flaws involved with the standard deviation, is that it depends on the units that are used. One way of handling this difficulty, is called the *coefficient of variation* which is the standard deviation divided by the mean times 100%

$$CV = \frac{\sigma}{\bar{x}} \times 100\%$$

In the above example, it is

$$\frac{17}{49.2} \times 100\% = 34.6\%$$

This tells us that the standard deviation of the restaurant bills is 34.6% of the mean.

**Q9. What do you mean by probability distribution?**

Ans. In probability theory and statistics, a probability distribution identifies either the probability of each value of a random variable (when the variable is discrete), or the probability of the value falling within a particular interval (when the variable is continuous). The probability distribution describes the range of possible values that a random variable can attain and the probability that the value of the random variable is within any (measurable) subset of that range.

**Q10. Describe Normal distribution.**

Ans. In probability theory, the normal (or Gaussian) distribution, is a continuous probability distribution that is often used as a first approximation to describe real-valued random variables that tend to cluster around a single mean value. The graph of the associated probability density function is "bell"-shaped, and is known as the Gaussian function or bell curve.

$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}},$$

where parameter  $\mu$  is the mean (location of the peak) and  $\sigma^2$  is the variance (the measure of the width of the distribution). The distribution with  $\mu = 0$  and  $\sigma^2 = 1$  is called the **standard normal**.

where parameter  $\mu$  is the mean (location of the peak) and  $\sigma^2$  is the variance (the measure of the width of the distribution). The distribution with  $\mu = 0$  and  $\sigma^2 = 1$  is called the standard normal.

The normal distribution is considered the most "basic" continuous probability distribution due to its role in the central limit theorem, and is one of the first continuous distributions taught in elementary statistics classes. Specifically, by the central limit theorem, under certain conditions the sum of a number of random variables with finite means and variances approaches a normal

distribution as the number of variables increases. For this reason, the normal distribution is commonly encountered in practice, and is used throughout statistics, natural sciences, and social sciences as a simple model for complex phenomena.

**Q11 . Difine Binomial Distribution.**

Ans. In probability theory and statistics, the binomial distribution is the discrete probability distribution of the number of successes in a sequence of  $n$  independent yes/no experiments, each of which yields success with probability  $p$ . Such a success/failure experiment is also called a Bernoulli experiment or Bernoulli trial. In fact, when  $n = 1$ , the binomial distribution is a Bernoulli distribution. The binomial distribution is the basis for the popular binomial test of statistical significance.

The binomial distribution gives the discrete probability distribution of obtaining exactly  $k$  successes out of  $n$  Bernoulli trials (where the result of each Bernoulli trial is true with probability  $p$  and false with probability  $1 - p$ ). The binomial distribution is therefore given by the formula:

In general, if the random variable  $K$  follows the binomial distribution with parameters  $n$  and  $p$ , we write  $K \sim B(n, p)$ . The probability of getting exactly  $k$  successes in  $n$  trials is given by the

**Probability mass function**

$$f(k; n, p) = \Pr(K = k) = \binom{n}{k} p^k (1 - p)^{n-k}$$

for  $k = 0, 1, 2, \dots, n$ , where

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

Where,

No. of trials= $n$

No. of success= $k$

Probability of success= $p$

Probability of failure= $q$

**Q12. Define Poisson Distribution.**

**Ans**

In probability theory and statistics, the Poisson distribution is a discrete probability distribution that expresses the probability of a number of events occurring in a fixed period of time if these events occur with a known average rate and independently of the time since the last event.

If the expected number of occurrences in this interval is  $\lambda$ , then the probability that there are exactly  $k$  occurrences ( $k$  being a non-negative integer,  $k = 0, 1, 2, \dots$ ) is equal to

$$\Pr(N_t = k) = f(k; \lambda t) = \frac{e^{-\lambda t} (\lambda t)^k}{k!}$$

where

- $e$  is the base of the natural logarithm ( $e = 2.71828\dots$ )
- $k$  is the number of occurrences of an event – the probability of which is given by the function
- $k!$  is the factorial of  $k$
- $\lambda$  is a positive real number, equal to the expected number of occurrences that occur during the given interval. For instance, if the events occur on average 4 times per minute, and one is interested in the probability of an event occurring  $k$  times in a 10 minute interval, one would use a Poisson distribution as the model with  $\lambda = 10 \times 4 = 40$ .

**Q13. What do you mean by Hypothesis Testing?**

**Ans**

Statistical hypothesis test is a method of making decisions using data, whether from a controlled experiment or an observational study (not controlled). In statistics, a result is called statistically significant if it is unlikely to have occurred by chance alone, according to a pre-determined threshold probability, the significance level.

**Q14 . Discuss the Z -test.**

**Ans.** The Z-test compares sample and population means to determine if there is a significant difference.

It requires a simple random sample from a population with a Normal distribution and where the mean is known.

The z measure is calculated as:

Suppose that in a particular geographic region, the mean and standard deviation of scores on a reading test are 100 points, and 12 points, respectively. Our interest is in the scores of 55 students in a particular school who received a mean score of 96. We can ask whether this mean score is significantly lower than the regional mean – that is, are the students in this school comparable to a simple random sample of 55 students from the region as a whole, or are their scores surprisingly low?

We begin by calculating the standard error of the mean:

$$SE = \frac{\sigma}{\sqrt{n}} = \frac{12}{\sqrt{55}} = \frac{12}{7.42} = 1.62$$

Next we calculate the z-score, which is the distance from the sample mean to the population mean in units of the standard error:

$$z = \frac{M - \mu}{SE} = \frac{96 - 100}{1.62} = -2.47$$

In this example, we treat the population mean and variance as known, which would be appropriate either if all students in the region were tested, or if a large

random sample were used to estimate the population mean and variance with minimal estimation error.

The classroom mean score is 96, which is  $-2.47$  standard error units from the population mean of 100. Looking up the  $z$ -score in a table of the standard normal distribution, we find that the probability of observing a standard normal value below  $-2.47$  is approximately  $0.5 - 0.4932 = 0.0068$ . This is the one-sided  $p$ -value for the null hypothesis that the 55 students are comparable to a simple random sample from the population of all test-takers. The two-sided  $p$ -value is approximately 0.014 (twice the one-sided  $p$ -value).

Another way of stating things is that with probability  $1 - 0.014 = 0.986$ , a simple random sample of 55 students would have a mean test score within 4 units of the population mean. We could also say that with 98% confidence we reject the null hypothesis that the 55 test takers are comparable to a simple random sample from the population of test-takers.

**Q15 . Discuss the uses of  $t$ -test.**

#### **Independent one sample $t$ -test**

In testing the null hypothesis that the population means is equal to a specified value  $\mu_0$ , one uses the statistic

$$t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}},$$

where  $s$  is the sample standard deviation of the sample and  $n$  is the sample size. The degrees of freedom used in this test is  $n - 1$ .

#### **Independent two-sample $t$ -test**

##### *Equal sample sizes, equal variance*

This test is only used when both:

- the two sample sizes (that is, the number,  $n$ , of participants of each group) are equal;
- it can be assumed that the two distributions have the same variance.

The  $t$  statistic to test whether the means are different can be calculated as follows:

$$t = \frac{\bar{X}_1 - \bar{X}_2}{S_{X_1X_2} \cdot \sqrt{\frac{2}{n}}}$$

where

$$S_{X_1X_2} = \sqrt{\frac{1}{2}(S_{X_1}^2 + S_{X_2}^2)}$$

Here  $S_{X_1X_2}$  is the grand standard deviation (or pooled standard deviation), 1 = group one, 2 = group two. The denominator of  $t$  is the standard error of the difference between two means.

For significance testing, the degrees of freedom for this test is  $2n - 2$  where  $n$  is the number of participants in each group.

#### *Unequal sample sizes, equal variance*

This test is used only when it can be assumed that the two distributions have the same variance. The  $t$  statistic to test whether the means are different can be calculated as follows:

$$t = \frac{\bar{X}_1 - \bar{X}_2}{S_{X_1X_2} \cdot \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

Where

$$S_{X_1X_2} = \sqrt{\frac{(n_1 - 1)S_{X_1}^2 + (n_2 - 1)S_{X_2}^2}{n_1 + n_2 - 2}}$$

Note that the formulae above are generalizations for the case where both samples have equal sizes (substitute  $n_1$  and  $n_2$  for  $n$  and you'll see).

$S_{X_1X_2}$  is an estimator of the common standard deviation of the two samples: it is defined in this way so that its square is an unbiased estimator of the common variance whether or not the population means are the same. In these formulae,  $n$  = number of participants, 1 = group one, 2 = group two.  $n - 1$  is the number of degrees of freedom for either group, and the total sample size minus two (that is,

$n_1 + n_2 - 2$ ) is the total number of degrees of freedom, which is used in significance testing.

*Unequal sample sizes, unequal variance*

This test is used only when the two population variances are assumed to be different (the two sample sizes may or may not be equal) and hence must be

$$t = \frac{\bar{X}_1 - \bar{X}_2}{s_{\bar{X}_1 - \bar{X}_2}}$$

estimated separately

where

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Where  $s^2$  is the unbiased estimator of the variance of the two samples,  $n$  = number of participants, 1 = group one, 2 = group two. Note that in this case,  $s_{\bar{X}_1 - \bar{X}_2}^2$  is not a pooled variance. For use in significance testing, the distribution of the test statistic is approximated as being an ordinary Student's t distribution with the degrees of freedom calculated using

$$\text{d.f.} = \frac{(s_1^2/n_1 + s_2^2/n_2)^2}{(s_1^2/n_1)^2/(n_1 - 1) + (s_2^2/n_2)^2/(n_2 - 1)}$$

**Q16 . Explain the use of Paired t-test.**

**Ans**

This test is used when the samples are dependent; that is, when there is only one sample that has been tested twice (repeated measures) or when there are two samples that have been matched or "paired". This is an example of a paired difference test.

$$t = \frac{\bar{X}_D - \mu_0}{s_D / \sqrt{n}}$$

For this equation, the differences between all pairs must be calculated. The pairs are either one person's pre-test and post-test scores or between pairs of persons matched into meaningful groups (for instance drawn from the same family or age

group: see table). The average ( $X_D$ ) and standard deviation ( $s_D$ ) of those differences are used in the equation. The constant  $\mu_0$  is non-zero if you want to test whether the average of the difference is significantly different from  $\mu_0$ . The degree of freedom used is  $n - 1$ .

**Q17.** Discuss the application of Chi -square test.

**Ans.** Chi-square is a statistical test commonly used to compare observed data with data we would expect to obtain according to a specific hypothesis. For example, if, according to Mendel's laws, you expected 10 of 20 offspring from a cross to be male and the actual observed number was 8 males, then you might want to know about the "goodness to fit" between the observed and expected. Were the deviations (differences between observed and expected) the result of chance, or were they due to other factors. How much deviation can occur before you, the investigator, must conclude that something other than chance is at work, causing the observed to differ from the expected. The chi-square test is always testing what scientists call the null hypothesis, which states that there is no significant difference between the expected and observed result.

The formula for calculating chi-square is:

The chi-square test is defined for the hypothesis:

H<sub>0</sub>: The data follow a specified distribution.

H<sub>a</sub>: The data do not follow the specified distribution.

Test For the chi-square goodness-of-fit computation, the test statistic is defined as

$$\chi^2 = \sum_{i=1}^k (O_i - E_i)^2 / E_i$$

where  $O_i$  is the observed frequency and  $E_i$  is the expected frequency.

**Q18.** What do you mean by Analysis of Variance?

**Ans.** An important technique for analyzing the effect of categorical factors on a response is to perform an Analysis of Variance. An ANOVA decomposes the variability in the response variable amongst the different factors. Depending upon the type of analysis, it may be important to determine: (a) which factors have a significant effect on the response, and/or (b) how much of the variability in the response variable is attributable to each factor.

1. One-Way ANOVA - used when there is only a single categorical factor. This is equivalent to comparing multiple groups of data.
2. Multifactor ANOVA - used when there is more than one categorical factor, arranged in a crossed pattern. When factors are crossed, the levels of one factor appear at more than one level of the other factors.

**Q19. What do you mean by Non Parametric Tests?**

*Ans.* *Non-parametric* tests cover techniques that do not rely on data belonging to any particular distribution. These include *distribution free* methods, which do not rely on assumptions that the data are drawn from a given probability distribution. As such it is the opposite of parametric statistics. It includes non-parametric statistical models, inference and statistical tests. Following are the nonparametric tests

**The Sign test**

The sign test is one of the simplest nonparametric tests. It is for use with 2 repeated (or correlated) measures and measurement is assumed to be at least ordinal. For each subject, subtract the 2nd score from the 1st, and write down the *sign* of the difference. (That is write "-" if the difference score is negative, and "+" if it is positive.) The usual null hypothesis for this test is that there is no difference between the two treatments. If this is so, then the number of + signs (or - signs, for that matter) should have a **binomial distribution** with  $p = .5$ , and  $N =$  the number of subjects. In other words, the sign test is just a binomial test with + and - in place of Head and Tail (or Success and Failure).

**Mann-Whitney U Test**

The *null hypothesis* assumes that the two sets of scores are samples from the same population; and therefore, because sampling was random, the two sets of scores *do not differ systematically* from each other. The *alternative hypothesis*, on the other hand, states that the two sets of scores *do differ systematically*.

### Runs test

The **runs test** (also called **Wald-Wolfowitz test** after Abraham Wald and Jacob Wolfowitz) is a non-parametric statistical test that checks a randomness hypothesis for a two-valued data sequence. More precisely, it can be used to test the hypothesis that the elements of the sequence are mutually independent.

### Rank sum test

The t-test is the standard test for testing that the difference between population means for two non-paired samples are equal. If the populations are non-normal, particularly for small samples, then the t-test may not be valid. The rank sum test is an alternative that can be applied when distributional assumptions are suspect.

**Q20. Discuss the use of Rank Correlation.**

**Ans**

When the distribution of variables is not Normal, the degree of relationship between the variables can be determined using Rank correlation. Instead of using the precise values of the variables, the data are ranked in order of size, and calculations are based on the differences between the ranks of corresponding values X and Y.

**Q21. Explain the calculation of Rank Correlation.**

**Ans**

In this example, we will use the raw data in the table below to calculate the correlation between the IQ of a person with the number of hours spent in front of TV per week.

IQ,  $X_i$  Hours of TV per week,  $Y_i$

106 7

86 0

100	27
101	50
99	28
103	29
97	20
113	12
112	6
110	17

First, we must find the value of the term  $d_i^2$ . To do so we use the following steps, reflected in the table below.

1. Sort the data by the first column ( $X_i$ ). Create a new column  $x_i$  and assign it the ranked values  $1, 2, 3, \dots, n$ .
2. Next, sort the data by the second column ( $Y_i$ ). Create a fourth column  $y_i$  and similarly assign it the ranked values  $1, 2, 3, \dots, n$ .
3. Create a fifth column  $d_i$  to hold the differences between the two rank columns ( $x_i$  and  $y_i$ ).
4. Create one final column  $d_i^2$  to hold the value of column  $d_i$  squared.

IQ, $X_i$	Hours of TV per week, $Y_i$	rank $x_i$	rank $y_i$	$d_i$	$d_i^2$
86	0	1	1	0	0
97	20	2	6	-4	16
99	28	3	8	-5	25

100	27	4	7	-3	9
101	50	5	10	-5	25
103	29	6	9	-3	9
106	7	7	3	4	16
110	17	8	5	3	9
112	6	9	2	7	49
113	12	10	4	6	36

The value of  $n$  is 10. So these values can now be substituted back into the equation,

$$\rho = 1 - \frac{6 \times 194}{10(10^2 - 1)}$$

Which evaluates to  $\rho = -0.175757575...$  This low value shows that the correlation between IQ and hours spent watching TV is very low.

## Chapter 7

# Bibliography and Report writing

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**Q1.** What do you mean by Bibliography?

**Ans.** A bibliography is a list of writings that share a common factor: this may be a topic, a language, a period, or some other theme. The list may be comprehensive or selective. One particular instance of this is the list of sources used or considered in preparing a work, sometimes called a reference list.

Citation formats vary, but an entry for a book in a bibliography usually contains the following information:

- author(s)
- title
- publisher
- date of publication

An entry for a journal or periodical article usually contains:

- author(s)
- article title
- journal title
- volume
- pages
- date of publication

**Q2. Discuss the process of Report Writing.**  
**Ans GUIDELINES FOR REPORT WRITING**

**1. Title Page.** First page of report. Try to find a title that clearly describes the work you have done and be as precise as possible. Mention your name, role number, guide's (and co-guide's) name, name of the department (i.e. Energy Systems Engineering), name of the institute, place and month and year of the report.

**2. Abstract.** On a separate page, immediately following the title page, summarize the main points of the report. Persons getting interested in the report after reading the title, should be able to judge from the abstract whether the report is really interesting for them.

**3. Table of Contents (TOC).** Should list only those items that follow it appearing in the following order.

- List of tables (1.1, 1.2, 1.3., 2.1, 2.2, .. etc.)
- List of figures (1.1, 1.2, 1.3., 2.1, 2.2, .. etc.)
- The chapters (1, 2, ... N, followed by the name of the chapter),
- Sections within chapters (e.g. 1.1, 2.4, etc. + name)
- Appendices (I, II, III, IV, .. etc. + name), if any
- References
- Acknowledgements

**4. The Chapters.** The number of chapters you need and their contents strongly depend on the topic selected and the subject matter to be presented. Roughly the following chapters may be included. However, it is your own report and you have to structure it according to the flow of overall logic and Organization.

Introduction

- Literature Survey.
- Theory-Oriented Chapters
- Practice-Oriented Chapters.
- Conclusions.

**5. References.**

**6. The Appendices.** Appendices are useful for those things that you consider important, but that do not fit in the main presentation of your work

**Case study**

**Q1** A die is thrown 132 times with the following results

No. turned up	1	2	3	4	5	6
Frequency	16	20	25	14	29	28

Is the die unbiased?

**Case 2** Set up ANOVA table for the following information relating to three drugs testing to judge the effectiveness in reducing blood pressure for three different groups of people;

Amount of Blood pressure reduction in Millimeters of Mercury

Group of people	X	Y	Z
A	14	10	11
	15	9	11
B	12	7	10
	11	8	11
C	10	11	8
	11	11	7

Do the drugs act differently?

Are the different groups of people affected differently?

Is the interaction term significant?

Answer the above question taking a significant level of 5%?

**CASE 3**

The mean produce of wheat of a sample of 100 fields in 200Ibs per care with a standard deviation of 10Ibs. Another sample of 150 fields gives the mean of 220Ibs. With the standard deviation of 12Ibs. Can the two samples be considered to have been taken from the same population whose standard deviation is 11 Ibs ? use 5percent level of significance?

**Case 4** an experiment is conducted to judge the effect of brand name on quality perception. 16 subjects are recruited for the purpose and asked to taste and compare two samples of product on a set of scale items to judge to be ordinal. The following data are obtained:

Pair	Brand A	Brand B
1	73	51
2	43	41
3	47	43
4	53	41
5	58	47
6	47	32
7	52	24
8	58	58
9	38	43
10	61	53
11	56	52
12	56	57
13	34	44
14	55	57
15	65	40
16	75	68

Test the hypothesis using Wilcoxon matched pairs test, that there is no difference between the perceived qualities of the two samples. Use 5% level of significance.

#### **Case 5**

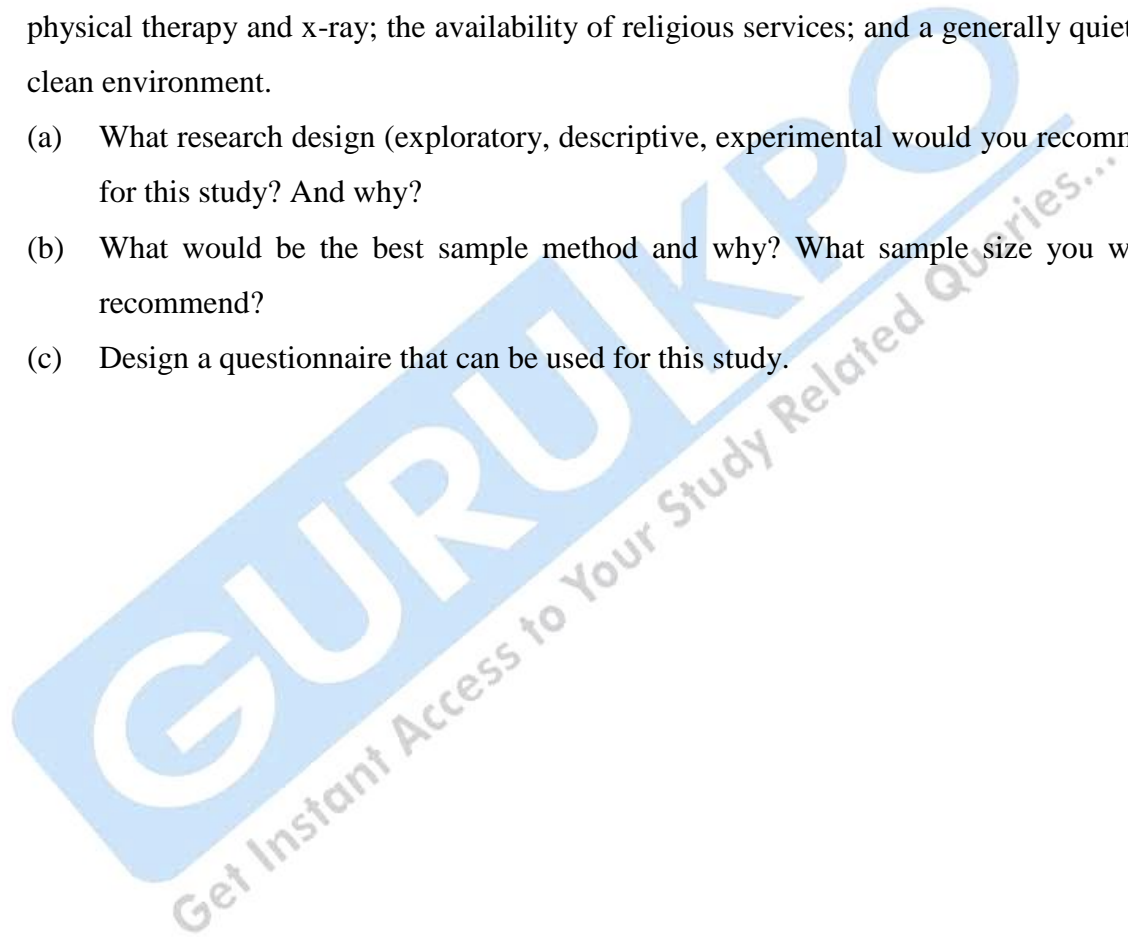
Solve the questions that follow the case study.

The administrators of Soni Hospital, Jaipur one of the city's largest, are interested to know the attitudes of the patients towards various aspects of the hospital after a stay of approximately one week or longer. The hospital administrators are specifically interested in the attitudes of those patients who have been treated in the hospital from 01, April 2006

onwards till today and on average 2500 patients are treated in the hospital. Out of this almost 35 percent patients stay beyond one week in the hospital for treatment.

They have authorized the undertaking of a marketing research study to gather this, and have directed that it covers the following areas : All administrative functions with which patients come into contact (such as admitting, billing and so on); the treatment and attitudes of interns and doctors; the food service and general housekeeping; the attention of nurses and nurse's aides; the courtesy and care of personnel in such departments as physical therapy and x-ray; the availability of religious services; and a generally quiet and clean environment.

- (a) What research design (exploratory, descriptive, experimental) would you recommend for this study? And why?
- (b) What would be the best sample method and why? What sample size would you recommend?
- (c) Design a questionnaire that can be used for this study.



**Multiple Choice Questions**

1. According to your text, how many points should a rating scale have?
  - a. Five
  - b. Four
  - c. Ten
  - d. Somewhere from 4 to 11 points
  
2. What is the problem(s) with this set of response categories to the question “What is your current age?”  
1-5    5-10    10-20    20-30    30-40
  - a. The categories are not mutually exclusive
  - b. The categories are not exhaustive
  - c. Both a and b are problems
  - d. There is no problem with the above set of response categories
  
3. You should mix methods in a way that provides complementary strengths and non overlapping weaknesses. This is known as the fundamental principle of mixed research
  - a. True
  - b. False
  
4. According to the text, questionnaires can address events and characteristics taking place when?
  - a. In the past (retrospective questions)
  - b. In the present (current time questions)
  - c. In the future (prospective questions)
  - d. All of the above
  
5. Which of the following are principles of questionnaire construction?
  - a. Consider using multiple methods when measuring abstract constructs
  - b. Use multiple items to measure abstract constructs
  - c. Avoid double-barreled questions
  - d. All of the above
  - e. Only b and c
  
6. Which of these is not a method of data collection
  - a. Questionnaires
  - b. Interviews

- c. Experiments
  - d. Observations
7. Secondary/existing data may include which of the following?
- a. Official documents
  - b. Personal documents
  - c. Archived research data
  - d. All of the above
8. An item that directs participants to different follow-up questions depending on their response is called a \_\_\_\_\_.
- a. Response set
  - b. Probe
  - c. Semantic differential
  - d. Contingency question
9. Which of the following terms best describes data that were originally collected at an earlier time by a different person for a different purpose?
- a. Primary data
  - b. Secondary data
  - c. Experimental data
  - d. Field notes
10. Researchers use both open-ended and closed-ended questions to collect data. Which of the following statements is true?
- a. Open-ended questions directly provide quantitative data based on the researcher's predetermined response categories
  - b. Closed-ended questions provide quantitative data in the participant's own words
  - c. Open-ended questions provide qualitative data in the participant's own words
  - d. Closed-ended questions directly provide qualitative data in the participants' own words
11. Open-ended questions provide primarily \_\_\_\_\_ data.
- a. Confirmatory data
  - b. Qualitative data
  - c. Predictive data
  - d. None of the above

12. Which of the following is true concerning observation?
- It takes less time than self-report approaches
  - It costs less money than self-report approaches
  - It is often not possible to determine exactly why the people behave as they do
  - All of the above
13. Qualitative observation is usually done for exploratory purposes; it is also called \_\_\_\_\_ Observation.
- Structured
  - Naturalistic
  - Complete
  - Probed
14. As discussed in chapter 6, when constructing a questionnaire it is important to do each of the following except \_\_\_\_\_.
- Use "leading" or "loaded" questions
  - Use natural language
  - Understand your research participants
  - Pilot your test questionnaire
15. Another name for a Likert Scale is a(n):
- Interview protocol
  - Event sampling
  - Summated rating scale
  - Ranking
16. Which of the following is not one of the six major methods of data collection that are used by educational researchers?
- Observation
  - Interviews
  - Questionnaires
  - Checklists
17. The type of interview in which the specific topics are decided in advance but the sequence and wording can be modified during the interview is called:
- The interview guide approach
  - The informal conversational interview
  - A closed quantitative interview
  - The standardized open-ended interview

18. Which one of the following is not a major method of data collection:
  - a. Questionnaires
  - b. Interviews
  - c. Secondary data
  - d. Focus groups
  - e. All of the above are methods of data collection
  
19. A question during an interview such as “Why do you feel that way?” is known as a:
  - a. Probe
  - b. Filter question
  - c. Response
  - d. Pilot
  
20. A census taker often collects data through which of the following?
  - a. Standardized tests
  - b. Interviews
  - c. Secondary data
  - d. Observations
  
21. The researcher has secretly placed him or herself (as a member) in the group that is being studied. This researcher may be which of the following?
  - a. A complete participant
  - b. An observer-as-participant
  - c. A participant-as-observer
  - d. None of the above
  
22. Which of the following is not a major method of data collection?
  - a. Questionnaires
  - b. Focus groups
  - c. Correlation method
  - d. Secondary data
  
23. Which type of interview allows the questions to emerge from the immediate context or Course of things?
  - a. Interview guide approach
  - b. Informal conversational interview
  - c. Closed quantitative interview
  - d. Standardized open-ended interview

24. When conducting an interview, asking "Anything else?, What do you mean?, Why do you feel that way?," etc, are all forms of:
- Contingency questions
  - Probes
  - Protocols
  - Response categories
25. When constructing a questionnaire, there are 15 principles to which you should adhere. Which of the following is not one of those principles?
- Do not use "leading" or "loaded" questions
  - Avoid double-barreled questions
  - Avoid double negatives
  - Avoid using multiple items to measure a single construct
26. Which of the following statements is false?
- The  $t$  distribution is symmetric about zero
  - The  $t$  distribution is more spread out than the standard normal distribution
  - As the degrees of freedom get smaller, the  $t$ -distribution's dispersion gets smaller
  - The  $t$  distribution is mound-shaped
27. For statistical inference about the mean of a single population when the population standard deviation is unknown, the degrees for freedom for the  $t$  distribution equal  $n-1$  because we lose one degree of freedom by using the:
- sample mean as an estimate of the population mean
  - sample standard deviation as an estimate of the population standard deviation
  - sample proportion as an estimate of the population proportion
  - sample size as an estimate of the population size
28. For a sample of size 20 taken from a normally distributed population with standard deviation equal to 5, a 90% confidence interval for the population mean would require the use of:
- $t = 1.328$
  - $t = 1.729$
  - $t = 2.12$
  - $z = 1.645$
29. Under which of the following circumstances is it impossible to construct a confidence interval for the population mean?
- A non-normal population with a large sample and an unknown population variance
  - A normal population with a large sample and a known population variance
  - Non-normal population with a small sample and an unknown population variance
  - A normal population with a small sample and an unknown population variance

30. Suppose that a one-tail  $t$  test is being applied to find out if the population mean is less than 100. The level of significance is .05 and 25 observations were sampled. The rejection region is:
- $t > 1.708$
  - $t < -1.711$
  - $t > 1.318$
  - $t < -1.316$
31. Which of the following is true about the  $t$  distribution?
- Approaches the normal distribution as its degrees of freedom increase
  - Assumes the population is normally distributed
  - It is more spread out than the standard normal distribution
  - All of the above statements are true
32. A random sample of size 20 taken from a normally distributed population resulted in a sample variance of 32. The lower limit of a 90% confidence interval for the population variance would be:
- 52.185
  - 20.375
  - 20.170
  - 54.931
33. A random sample of size 15 taken from a normally distributed population revealed a sample mean of 75 and a sample variance of 25. The upper limit of a 95% confidence interval for the population mean would equal:
- 77.769
  - 72.231
  - 72.727
  - 77.273

**Answer**

- d
- c
- a
- d
- d

6. c

7. d

8. d

9. b

10. c

11. b

12. c

13. b

14. a

15. c

16. d

17. a

18. e

19. a

20. b

21. a

22. c

23. b

24. b

25. d

26. c

27. a

28. d

29. c



30.b

31.d

32.c



## Key Terms

**Research:** Research makes attempt to answer certain questions which have not answered till date. It generally explores the answer to those problems for which the answer can be given on the basis of available data. Thus research is a process to arrive at dependable solutions of the problems through a well planned method, means scientific method. This method of research is continuously advancing knowledge for promoting progress of the nation in all spheres of life.

**Variable:** A variable is an object, event, idea, feeling, time period, or any other type of category you are trying to measure. There are two types of variables-**independent and**

**dependent.** The "dependent variable" represents the output or effect, or is tested to see if it is the effect. The "independent variables" represent the inputs or causes, or are tested to see if they are the cause.

**Experiment :** The Process of examine the truth of a statistical hypotheses relating to some research problem is known as experiment.

**Probability: Probability** (or likelihood ) is a measure or estimation of how likely it is that something will happen or that a statement is true. Probabilities are given a value between 0 (0% chance or *will not happen*) and 1 (100% chance or *will happen*).The higher the degree of probability, the more likely the event is to happen, or, in a longer series of samples, the greater the number of times such event is expected to happen.

**Primary data** are collected by the investigator through field survey. Such data are in raw form **and** must be refined before use.

**Secondary Data:** secondary data are extracted from the existing published or u **Research**

**hypotheses** : are the predictive statement capable of being tested by scientific methods that relates an independent variable to some dependent variable.

**Probability distribution** : In probability theory and statistics, a probability distribution identifies either the probability of each value of a random variable (when the variable is discrete), or the probability of the value falling within a particular interval (when the variable is continuous). The probability distribution describes the range of possible values that a random variable can attain and the probability that the value of the random variable is within any (measurable) subset of that range.

**Range:** The range,  $R$ , of the data is the difference of the highest and smallest values.

**Non pragmatic test:** which do not rely on assumptions that the data are drawn from a given probability distribution.

**Deviation:** The deviation is the difference of each value from the mean. This is used in the calculation of the standard deviation and variance. " $x$ " is the point of interest. The sum of deviations from the mean is always zero.

**Mean:** Mean is the average of the numbers: a calculated "central" value of a set of numbers.

**Mode:** The **mode** is the value that appears most often in a set of data.

**Median:** The **median** of a set of data is the middlemost number in the set. The median is also the number that is halfway into the set. To find the median, the data should first be arranged in order from least to greatest.

**Standard deviation:** **standard deviation** (represented by the symbol sigma,  $\sigma$ ) shows how much variation or dispersion exists from the average (mean), or expected value.

